

## ELECTRICITY

Items 1-10 are multiple-choice with a single correct answer, and each is scored with 0.9 points (1 point awarded from start for this section).

Items 11 and 12 are scored independently with 4.5 points each (1 point awarded from start for this section)

Final score is calculated as:  $N = 0.6N_1 + 0.4N_2$ , unde

$N_1$  = score for the first section (items 1-10) + 1 point from start,

$N_2$  = score for the second section (items 11-12) + 1 point from start .

Working time – two hours.

1. At the terminals of a battery with electromotive voltage  $E$  and internal resistance  $r$ , an ideal ammeter is connected, indicating the current intensity  $I_0$ . By disconnecting the ideal ammeter and connecting an ammeter with internal resistance  $R_A$  across the battery terminals, it shows the current intensity  $I$ . The expressions for these two quantities are:

a) $I_0 = I = \frac{E}{r}$	b) $I_0 = \frac{E}{r}$ $I = \frac{E}{r + R_A}$	c) $I_0 = \frac{E}{r}$ $I = \frac{E}{R_A}$	d) $I_0 = I = \frac{E}{r + R_A}$
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2. What expression represents the maximum power delivered by a voltage source to a resistor with variable resistance? The electromotive voltage  $E$  of the source and its internal resistance  $r$  are known.

a) $P_{max} = \frac{E^2}{r}$	b) $P_{max} = \frac{2E^2}{r}$	c) $P_{max} = \frac{E^2}{4r}$	d) $P_{max} = \frac{4E^2}{r}$
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3. Which statement is correct?

a) The current intensity is a vector quantity	b) The electric power is a vector quantity	c) The electric charge is a vector quantity	d) The force is a vector quantity
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4. A student conducts an experiment in which he measures the voltage across a metallic resistor through which a current is flowing and finds a value of 2V. Knowing that the power dissipated in the conductor is 2W, determine the electric current intensity through the conductor.

a) $I = 1 \text{ A}$	b) $I = 2 \text{ A}$	c) $I = 3 \text{ A}$	d) $I = 4 \text{ A}$
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5. Three identical light bulbs are connected in parallel across the terminals of an ideal battery. If a fourth light bulb, identical to the first three, is added in parallel across the battery terminals, then:

a) The voltage across the battery terminals decreases	b) The current intensity through the battery decreases	c) The voltage across the battery terminals does not change	d) The current intensity through the battery does not change
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6. On a resistor with a resistance of  $5\Omega$ , a voltage of 10V is applied. What is the current intensity through the conductor?

a) 2 A	b) 50 A	c) 0,5 A	d) 15 A
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7. A cylindrical conductor with a cross-sectional area of  $1\text{mm}^2$  carries a intensity of 1A. The concentration of conduction electrons is  $n = 10^{28}\text{m}^{-3}$ , and the elementary electric charge is  $e = 1.6 \times 10^{-19} \text{ C}$ . What average speed has the ensemble of conduction electrons?

a) $0,625 \text{ mm} \cdot \text{s}^{-1}$	b) $1,6 \times 10^8 \text{ m} \cdot \text{s}^{-1}$	c) $3 \times 10^8 \text{ m} \cdot \text{s}^{-1}$	d) $100 \text{ km} \cdot \text{h}^{-1}$
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8. A cylindrical resistor made of a material with the electrical resistivity  $\rho$ , has length  $l$  and cross-sectional area  $S$ . Its electrical resistance can be expressed as follows:

a) $R = \rho S l$	b) $R = \frac{\rho l}{S}$	c) $R = \frac{\rho S}{l}$	d) $R = \frac{1}{\rho l S}$
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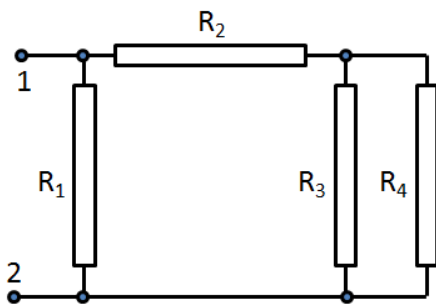
9. The electrical energy consumed during  $\Delta t=1\text{s}$  by a resistor of  $1\Omega$  traversed by a current of  $1\text{A}$  is:

a) $W = RI \Delta t = 1\text{J}$	b) $W = R^2 I \Delta t = 1\text{J}$	c) $W = I^2 R \Delta t^2 = 1\text{J}$	d) $W = UI \Delta t = 1\text{J}$
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10. During a time of  $1\text{s}$ , an arbitrary section of some conductor is traversed by an electric charge of  $1\text{C}$ . The average current flowing in the conductor is:

a) $I = Q \Delta t = 1\text{A}$	b) $I = \frac{Q}{\Delta t} = 1\text{A}$	c) $I = \frac{\Delta t}{Q} = 1\text{A}$	d) $I = \sqrt{\frac{Q}{\Delta t}} = 1\text{A}$
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11. (4.5p) The setup in the figure has  $R_1 = n_1\Omega$ ,  $R_2 = n_2\Omega$ ,  $R_3 = n_3\Omega$ ,  $R_4 = n_4\Omega$ , with  $n_1, n_2, n_3$  and  $n_4$  integers, solutions to the quadratic equations  $x^2 - b_1x + 21 = 0$  or  $x^2 - b_2x + 21 = 0$ .



(a) What minimum value  $R_{\min}$  can the equivalent resistance between terminals 1 and 2 have? (1p)

(b) What maximum value  $R_{\max}$  can the equivalent resistance between terminals 1 and 2 have? (1p)

(c) Under the conditions of (a), an ideal dc voltage source with e.m.f.  $E = 10\text{V}$  is connected to terminals 1 and 2. What intensities  $I_3, I_4$  flow through  $R_3, R_4$ ? (1.5p)

(d) What is the minimum value  $R_{\min}^{\square}$  of the equivalent resistance of a setup (different from the one in the figure) in which all four resistances are mandatory used? (1p)

12. (4.5p) Some amount of water with the initial temperature  $T_0$  is brought to a boil after  $\Delta t_1 = 10\text{min}$ . using an electric kettle with the electric resistance  $R_1$  and its efficiency  $\eta_1 = 0.5$ .

(a) What is  $R_2$  of a kettle with an efficiency  $\eta_2 = 0.8$  that boils the same amount of water in  $\Delta t_2 = 20\text{min}$ ? (1p)

(b) If both kettles are used *simultaneously* to boil the water, what is the *time interval*  $\Delta t_3$ ? (1p)

(c) If both kettles are used *simultaneously*, their resistors being connected in parallel, *how long*  $\Delta t_4$  will it take to bring the water to a boil? (1p)

(d) What is the *efficiency*  $\eta$  of using kettles under the conditions of point (c)?

Note: The initial temperature  $T_0$  of the water is always the same. (1.5p)